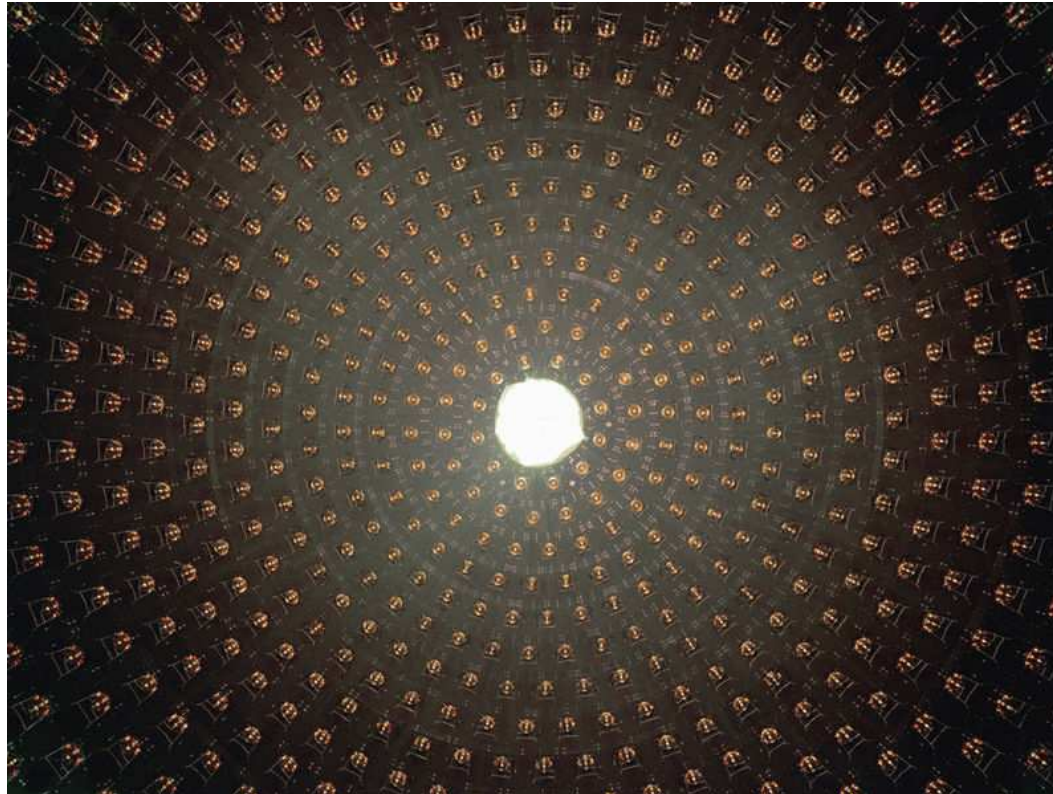


Searching for Sterile Neutrinos from π/K Decays



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[arXiv:1208.5559](https://arxiv.org/abs/1208.5559)

Hints of “sterile” neutrinos

- Possibly more than 3 mass eigenstates.

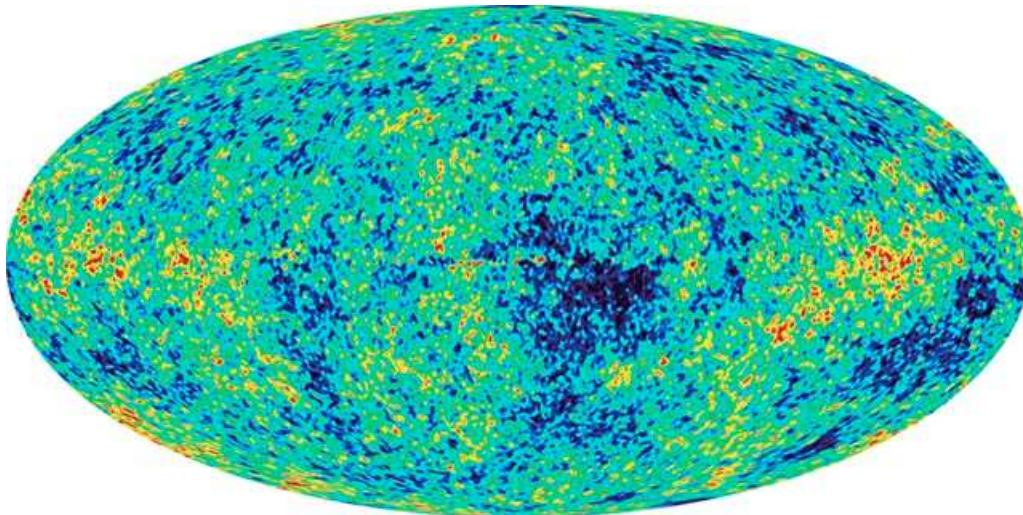
$$\Psi_{\nu\alpha} = \sum_j U_{\alpha j} \Psi_{\nu j}$$

- SBL Oscillation experiments:

- LSND(1), MiniBooNE(2), reactor anomalies. (W. Louis’ talk)
- Suggests 4th mass \sim O(eV). Not without tension.

- Cosmology:

- Planck/WMAP $N_{\text{eff}} > 3$? Details of sterile thermalization needed. (C. Lunardini’s talk)
- Small scale structure: Warm dark matter. A \sim 1keV WDM candidate is a potential solution for small scale problem (CDM produces too many substructures)(3)



- 1) Aguilar et. al. (LSND) Phys. Rev. D64, 112007 (2001)
- 2) MiniBooNE collaboration, Phys. Rev. Lett. 105,181801 (2010)
- 3) Abazajian et al. arXiv:1204.5379

Decay at Rest – Detecting Heavy Steriles

$$q^* = \frac{1}{2m_M} \left[(m_M^2 - (m_l + m_s)^2)(m_M^2 - (m_l - m_s)^2) \right]^{\frac{1}{2}} ; m_s \leq m_M - m_l$$

- Presence of sterile neutrinos implies monochromatic peaks in lepton spectrum (Schrock 1980). Difficult to resolve peaks.
- Massless neutrinos have fixed helicity, cannot boost ahead.



Pion decay at rest with resulting helicity. (Griffiths: Particle Phys)

- Only mention of wrong helicity proposed search requires searching from already identified peaks. Partial decay widths obtained by standard techniques.

$$\Gamma_{\pi/K \rightarrow l \bar{\nu}_s}^{++} = \frac{G_F^2}{4\pi} |U_{ls}|^2 |V_{ud/us}|^2 f_{\pi/K}^2 q^* m_l^2 \left[\frac{E_{\nu_s}(q^*) + q^*}{E_l(q^*) + q^*} \right]$$

$$\Gamma_{\pi/K \rightarrow l \bar{\nu}_s}^{--} = \frac{G_F^2}{4\pi} |U_{ls}|^2 |V_{ud/us}|^2 f_{\pi/K}^2 q^* m_{\nu_s}^2 \left[\frac{E_l(q^*) + q^*}{E_{\nu_s}(q^*) + q^*} \right]$$

Decay at Rest – Heavy Steriles

$$Br_{M \rightarrow l \bar{\nu}_s}^{--} \equiv \frac{\Gamma_{M \rightarrow l \bar{\nu}_s}^{--}}{\Gamma_M^{tot}} = |U_{ls}|^2 \frac{2 Br(M \rightarrow \mu \bar{\nu}) q^* m_{\nu_s}^2 \left[\frac{E_l(q^*) + q^*}{E_{\nu_s}(q^*) + q^*} \right]}{m_\mu^2 m_M \left(1 - \frac{m_\mu^2}{m_M^2}\right)^2}$$

$$Br_{K \rightarrow \mu, e \bar{\nu}_s}^{--} \lesssim 10^{-9} - 10^{-6} \text{ for } \begin{cases} 4 \text{ MeV} \lesssim m_s \lesssim 360 \text{ MeV} (\mu - \text{channel}) \\ 4 \text{ MeV} \lesssim m_s \lesssim 414 \text{ MeV} (e - \text{channel}) \end{cases}$$

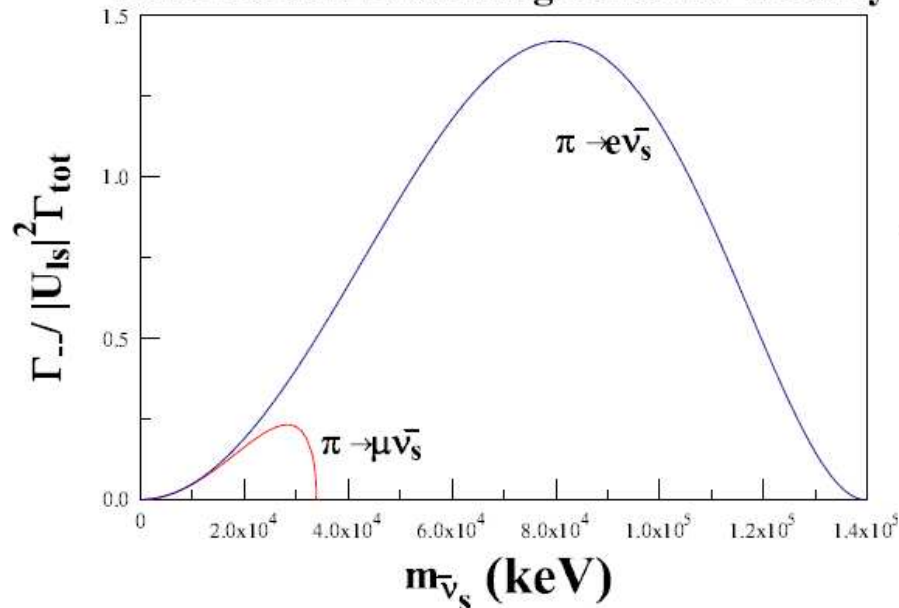
- Left handed branching ratio unique to massive neutrinos. Helpful for HEAVY sterile

- Spatially separate via Stern Gerlach. Complimentary with searches for monochromatic peaks.

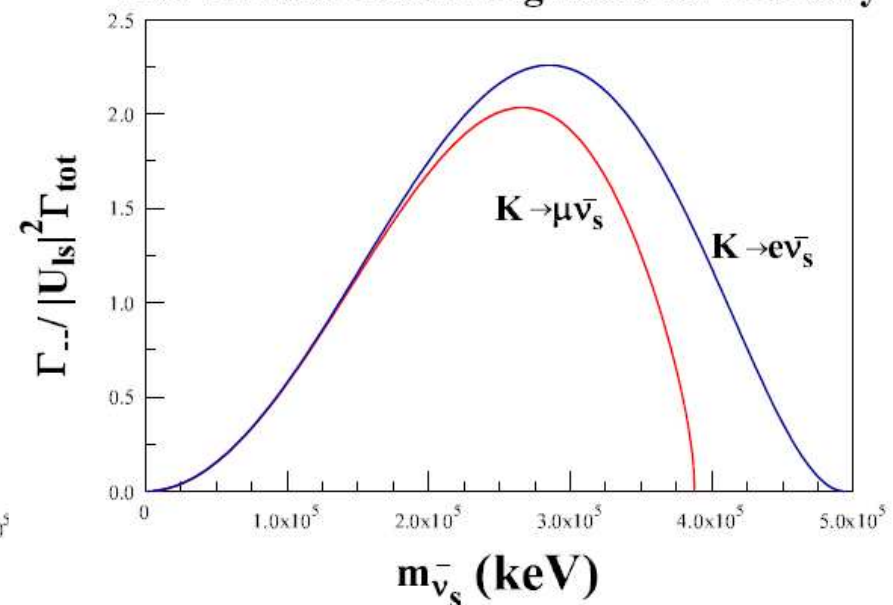
- Bound BR with U bounds*

*Kusenko, Pscoli, Semikov, JHEP 0511, 028 (2005)

Left Handed Branching Ratio for π Decay



Left Handed Branching Ratio for K Decay



Left handed branching ratio for pion/kaon DAR

Standard Treatment Of Neutrino Oscillations

$$\langle \nu_\alpha | e^{-iHt} | \nu_\beta(t) \rangle = \sum_i U_{\alpha i}^* U_{\beta i} e^{-im_i \tau_i}$$

$$m_i \tau_i = E_i t - L p_i \cong E(t-L) + \frac{m_i^2}{2E} L$$

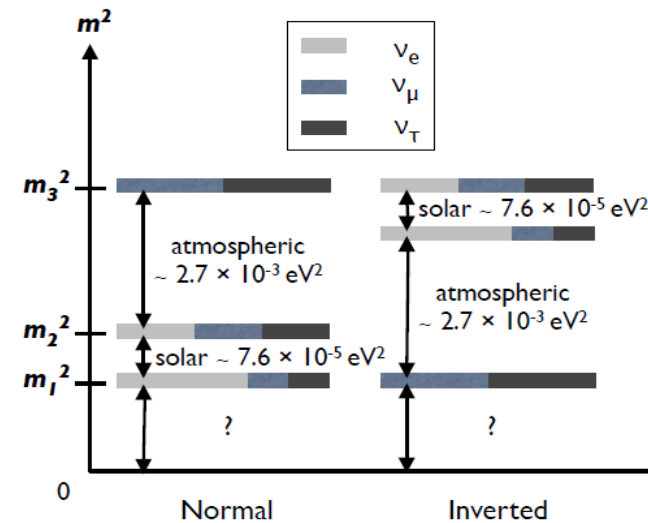
$$P(\nu_\alpha \rightarrow \nu_\beta) = \sum_{ij} U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* e^{-i \frac{\Delta m_{ij}^2 L}{2E}}$$

$$= \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left(\Delta m_{ij}^2 \frac{L}{4E} \right)$$

$$+ 2 \sum_{i>j} \text{Im}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin \left(\Delta m_{ij}^2 \frac{L}{2E} \right)$$

- Evolve initial state and boost to lab frame, assume $E \gg m$. Use unitarity for probability.

- Obtain neutrino composition through experiment



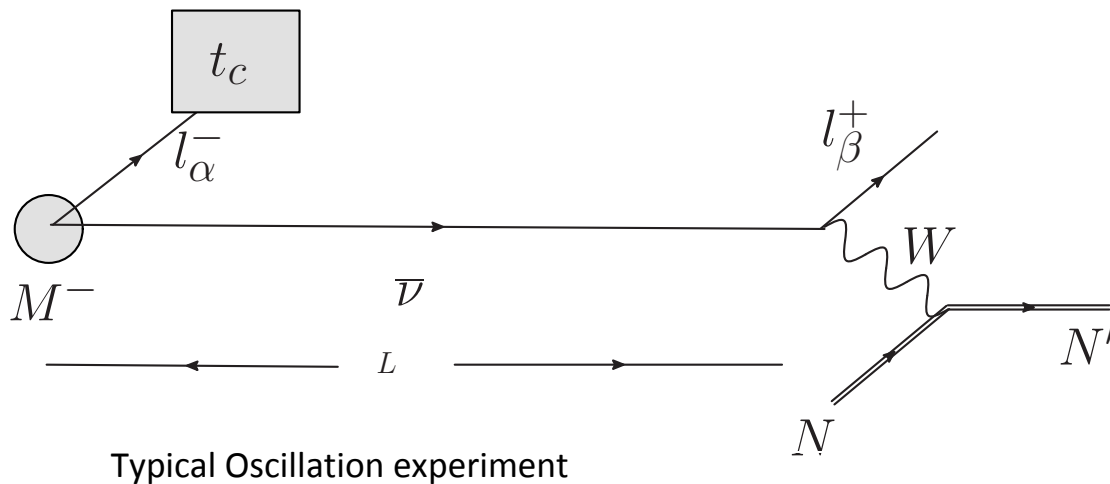
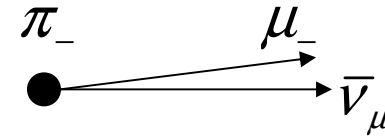
Mixing and mass compositions.

Shortcomings of standard treatment

- Doesn't account for production. Would expect lifetime and entanglement effects (however small they may be).

- Borrow the Wigner Weisskopf method ubiquitous in quantum optics (also used for K/ \bar{K} mixing).

- Typical accelerator experiment – muon (or e) is stopped at end of decay pipe.



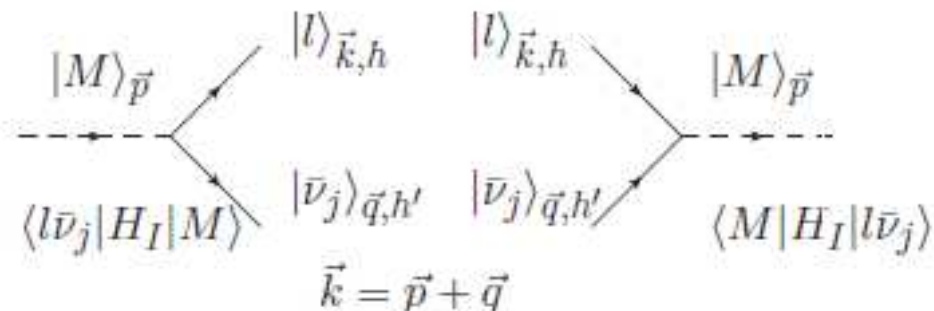
- Note: Will only discuss Dirac neutrinos. Majorana case is similar.

Wigner Weisskopf Theory (Sketch)

- Treat as initial value problem (ρ/K at $t=0$).
- Expand state in eigenstates of free H , obtain eq for coeff.

$$\frac{d}{dt} C_n(t) = -i \sum_m \langle n | H_I(t) | m \rangle C_m(t)$$

- Infinite hierarchy in principle. Cut hierarchy at 2 particle states.



- Derivative expansion in self energy. Keep up to leading order.
- Time dependent coefficients are obtained! (See paper for gory details)

Full Quantum State

- Full quantum state obtained using Wigner Weisskopf approx. Technical details: Lello, Boyanovsky [arXiv:1208.5559](https://arxiv.org/abs/1208.5559)
- Includes decay width of parent particle and entanglement. Decay width a la Fermi's Golden rule and one loop self energy are reproduced

Exact Entangled Quantum State

$$|M_{\bar{p}}^-(t)\rangle = e^{-iE_M(p)t} e^{-\Gamma_M(p)\frac{t}{2}} |M_{\bar{p}}^-(0)\rangle - F_M \sum_{\vec{q}, \alpha, j, h, h'} U_{\alpha j} \frac{\bar{U}_{\alpha, h}(\vec{k}) \gamma^\mu \hat{L} \mathcal{V}_{j, h'}(\vec{q}) p_\mu}{\sqrt{8VE_M(p)E_\alpha(k)E_j(q)}} \times$$

$$\left[\frac{1 - e^{-i(E_M^r(p) - E_\alpha(k) - E_j(q) - i\frac{\Gamma_M}{2})t}}{E_M^r(p) - E_\alpha(k) - E_j(q) - i\frac{\Gamma_M}{2}} \right] e^{-i(E_\alpha(k) + E_j(q))t} |l_\alpha^-(h, \vec{k})\rangle |\bar{v}_j(h', -\vec{q})\rangle$$

$$\lim_{\epsilon \rightarrow 0^+} i \frac{\sum |\langle M | \hat{H}_I(0) | \kappa \rangle|^2}{E_M - E_\kappa + i\epsilon} = i\Delta E_M + \frac{\Gamma_M}{2}$$

Propagating State

- Measure muon (or e) leaves true propagating neutrino state
- Recover original state when prefactors independent of mass

$$|\tilde{\nu}(\vec{q}, h_i)\rangle \equiv \langle l_{\alpha}^{-}(h_i, \vec{k}) | M_{\bar{p}}^{-}(t_c)\rangle$$

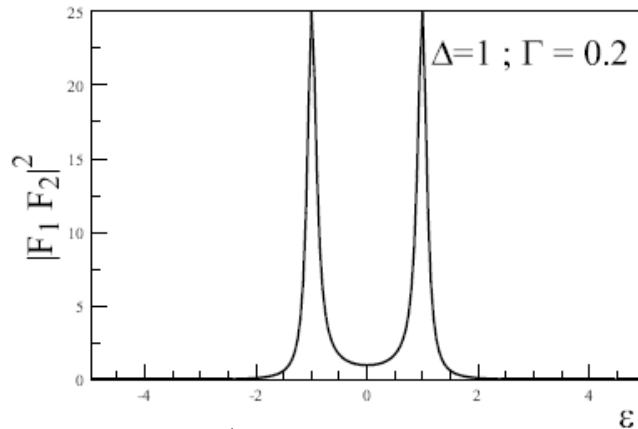
Propagating state

$$|\tilde{\nu}(\vec{q}; h_i)\rangle = -e^{-iE_{\alpha}(k)t_c} \sum_{j, h'} U_{\alpha j} \Pi_{\alpha j}^P \mathcal{M}_{\alpha j}^P(\vec{k}, \vec{q}, h_i, h') \mathcal{F}_{\alpha j}[\vec{k}, \vec{q}; t_c] e^{-iE_j(q)t_c} |\bar{\nu}_j(h', -\vec{q})\rangle$$

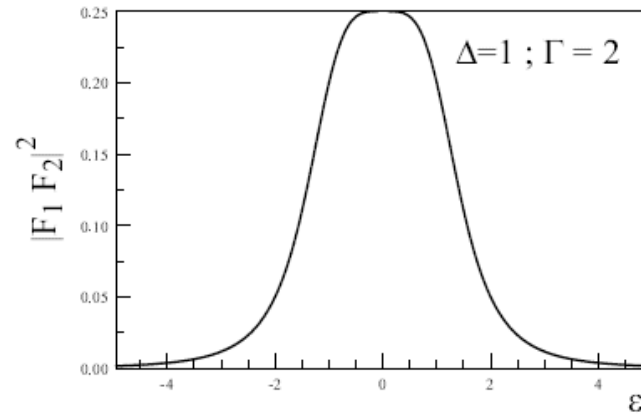
- Definitions obvious from full state. F is the important quantity.
- As expected, dependence on disentanglement scale, decay width
- Transition rate easily obtained from here. Interference contained in “F” terms
- Factorizes into production, propagation, detection

Qualitative Interpretation

- Intrinsic uncertainty in energy. $\Gamma \gg \Delta$ yields overlapping Lorentzians, reduces to usual Pontecorvo state. Large uncertainty blurs states together.
- Width of Lorentzian versus energy separation. Energy conservation in short width limit



$$E_\nu = \epsilon \pm \Delta$$



Product of Lorentzians when peak separation is greater(lesser) than decay width

- This is relevant for short baseline experiments. Long baseline focuses on much smaller mass differences.
- Corrections due to decay width and entanglement length scale are present as expected
- As $\Gamma L \ll 1$, recover original coherent picture.

Modifying Quantities

- Two important dimensionless quantities
- Bring about amplitude suppressions and phase shifts.

Important Scales:

$$\mathcal{R}_{ij} = \frac{\Delta_{ij}}{\Gamma_M(p)} = \frac{\delta m_{ij}^2}{2\Gamma_M M_M} \frac{E_M(p)}{E(q)}$$

Suppression and
phase shift

$$e^{-\Gamma_M(p)L_c}$$

Suppression

- Both are miniscule for reactors ($L \sim 0$, long lifetimes). Unchanged!

Modifying Oscillation Formula

- Main difference: Amplitude modification and phase shift
- Similar results in literature through different analysis*

Modified version in full glory:

$$\mathcal{P}_{\alpha \rightarrow \beta} = \delta_{\alpha, \beta} - 2 \sum_{j>i} \operatorname{Re}[U_{\alpha j} U_{\beta j}^* U_{\alpha i}^* U_{\beta i}] \operatorname{Re}[1 - I_{ij}] - 2 \sum_{j>i} \operatorname{Im}[U_{\alpha j} U_{\beta j}^* U_{\alpha i}^* U_{\beta i}] \operatorname{Im}[I_{ij}]$$

$$\operatorname{Re}[I_{ji}] = \frac{1}{\sqrt{1 + \mathcal{R}_{ji}^2}} \frac{1}{1 - e^{-\Gamma_M(p)L_c}} \left\{ \cos\left[\frac{\delta m_{ji}^2}{2E} L - \theta_{ji}(E)\right] - e^{-\Gamma_M(p)L_c} \cos\left[\frac{\delta m_{ji}^2}{2E} (L - L_c) - \theta_{ji}(E)\right] \right\}$$

$$\operatorname{Im}[I_{ji}] = \frac{1}{\sqrt{1 + \mathcal{R}_{ji}^2}} \frac{1}{1 - e^{-\Gamma_M(p)L_c}} \left\{ \sin\left[\frac{\delta m_{ji}^2}{2E} L - \theta_{ji}(E)\right] - e^{-\Gamma_M(p)L_c} \sin\left[\frac{\delta m_{ji}^2}{2E} (L - L_c) - \theta_{ji}(E)\right] \right\}$$

$$\cos[\theta_{ji}(E)] = \frac{1}{\sqrt{1 + \mathcal{R}_{ji}^2}} \quad ; \quad \sin[\theta_{ji}(E)] = \frac{\mathcal{R}_{ji}}{\sqrt{1 + \mathcal{R}_{ji}^2}}$$

* D. Hernandez, A. Yu. Smirnov, Phys.Lett. B706, 360 (2012)

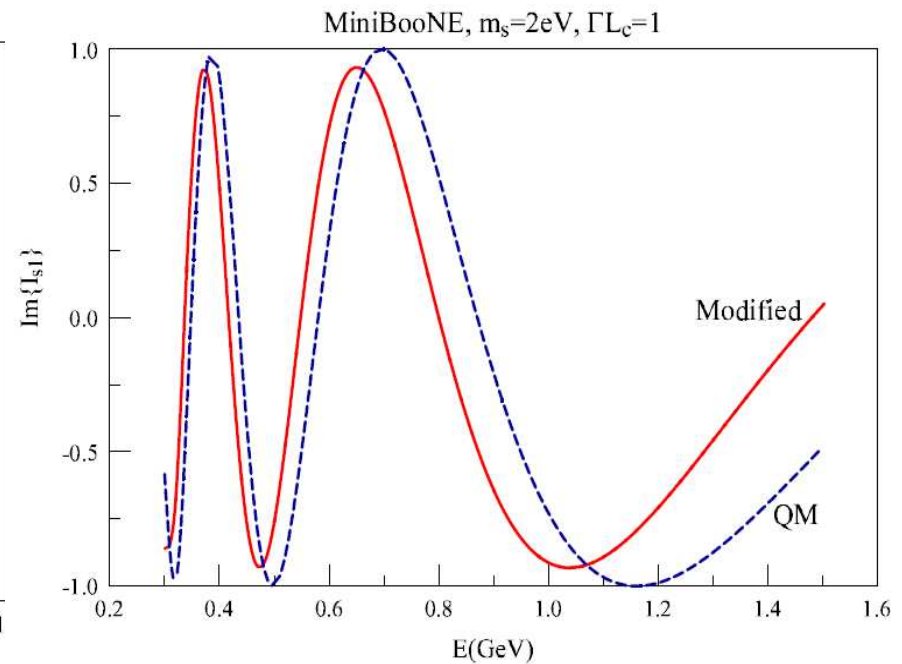
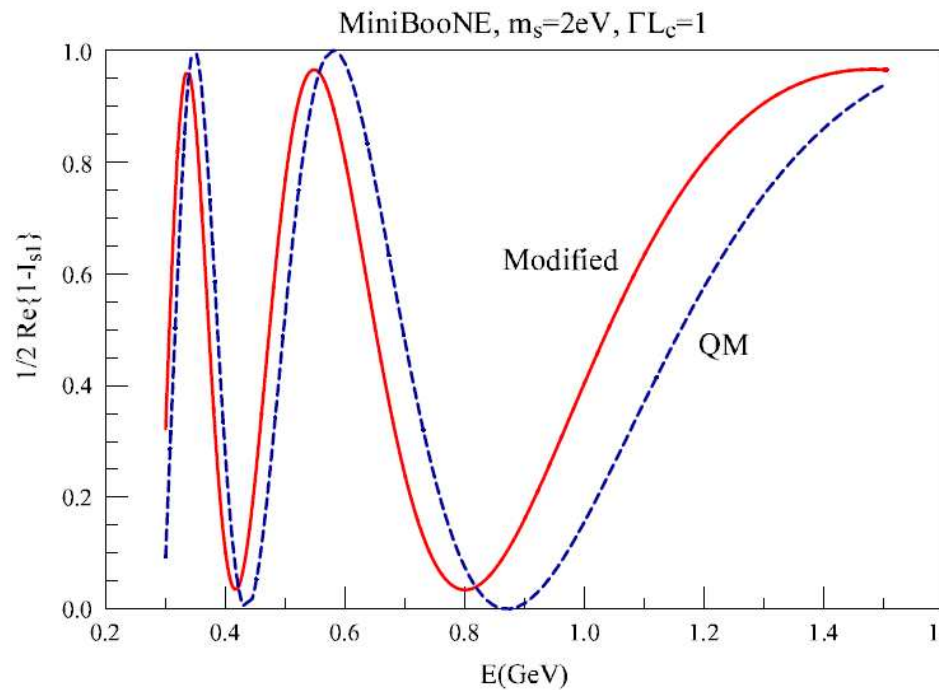
* E. Kh. Akhmedov, D. Hernandez, A. Yu. Smirnov, JHEP 1204, 052 (2012).

Present Accelerator Experiments: MiniBooNE

- Depending on sterile mass and *experimental parameters*, data may need further analysis.

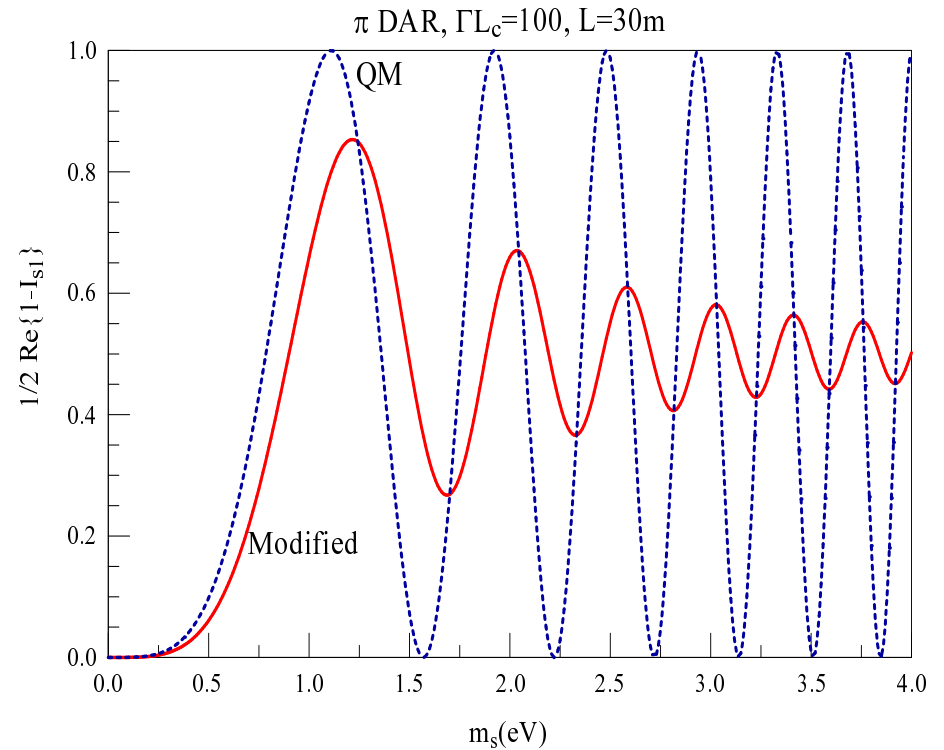
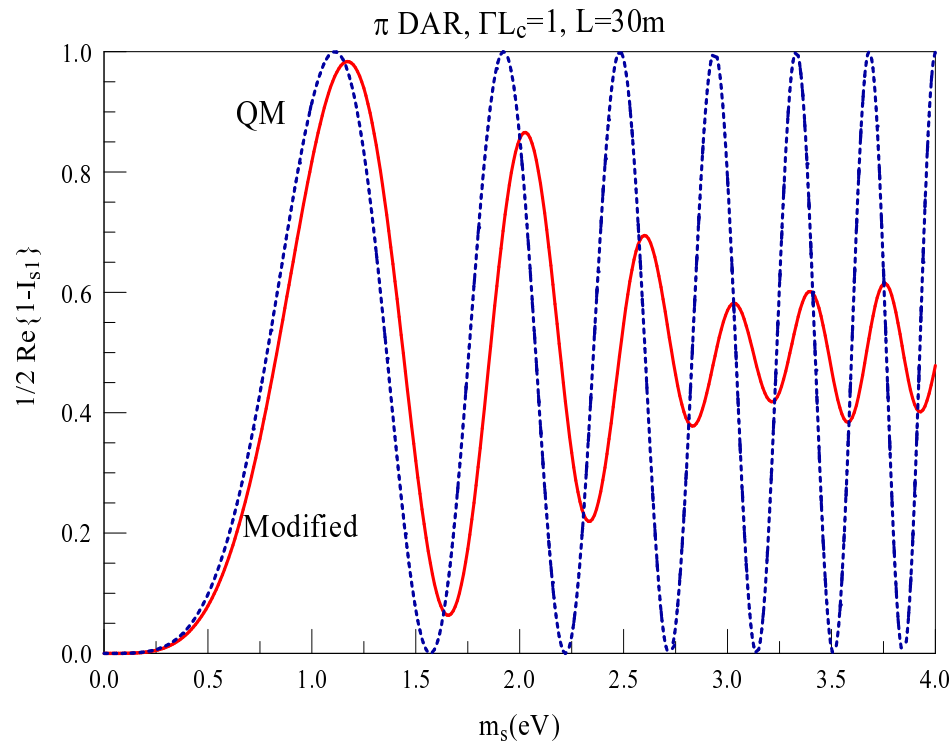
- MiniBooNE: Baseline $\sim 540\text{m}$, $E \sim 1\text{GeV}$, $\Gamma L_c \sim 1$. Sensitive to 1eV .

- $\sim 10\text{-}15\%$ modification to mass and angle. (3+1)



Decay at rest experiments

- Future proposed experiments seek to study decay at rest, potentially able to glean hints of sterile neutrinos
- Modifications to simple quantum mechanical picture are clear (for various ΓL)



Summary

- Heavy steriles might be found with combined searches for monochromatic lines and Stern-Gerlach experiment.
- Neutrino oscillations may decohere. Must control decay width and stopping distance to use (naive) QM formulae.
- Irrelevant for reactor experiments
- MiniBooNE would miss by $\sim 15\%$ for 3+1 with 1 eV sterile
- Keep in mind for next gen experiments.

Questions?? Comments??